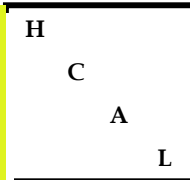




Energy Flow Within Jets

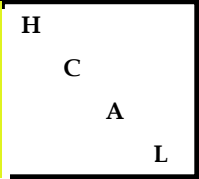


Dan Green
Fermilab

July, 2002



MLLA - Theory



$$dN / dy = (4/3) [\Gamma(B) / \pi] \int_{-\pi/2}^{\pi/2} d\tau e^{-B\alpha} \{ [\cosh \alpha + (1-2p) \sinh \alpha] / [4/3 Y(\alpha / \sinh \alpha)] \}^{B/2}$$

$$I_B(\sqrt{(16/3) Y \alpha / \sinh \alpha [\cosh \alpha + (1-2p) \sinh \alpha]})$$

$$y = \log(1/x), \quad x = 2k/M$$

$$Y = \log(2M \sin \theta_c / Q)$$

$$p = 1 - y/Y$$

$$\alpha = \alpha_o + i\tau$$

$$\tanh(\alpha_o) = (2p - 1)$$

$$B = 101/81$$

$$Q = 0.23 \text{ GeV}$$

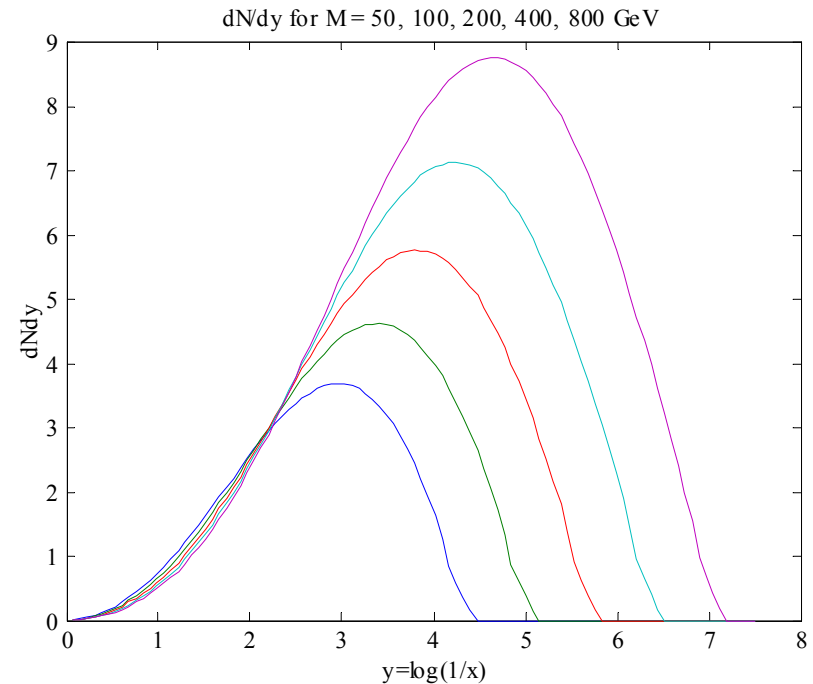
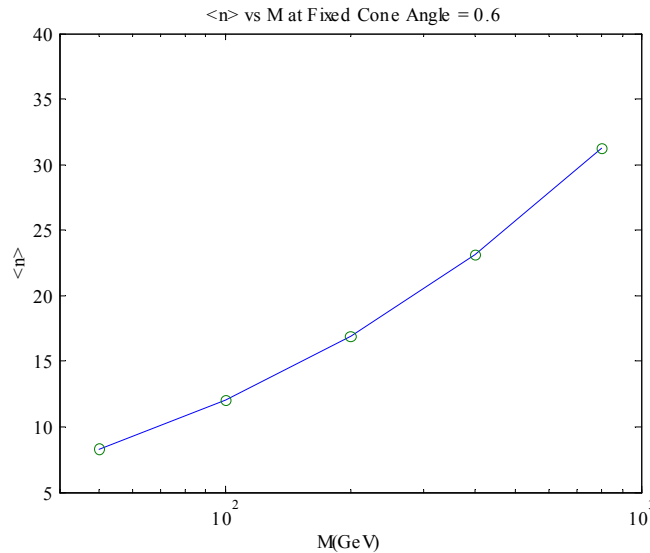
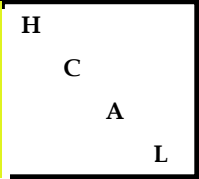
$$N = \Gamma(B)(z/2)^{1-B} I_{B+1}(z)$$

$$z = \sqrt{16/3(Y)}$$

QCD in LLA predicts the x distribution of partons. LPD then gives hadron distribution in x in terms of basically 1 parameter. The value of Q is taken from CDF fits to data. The theory appears in J. Mod Phys. A 1875 (1992) and Z Phys C, 55, 107 (1992). The CDF fits appear in Fermilab - Pub - 02/096-E (June 2002).



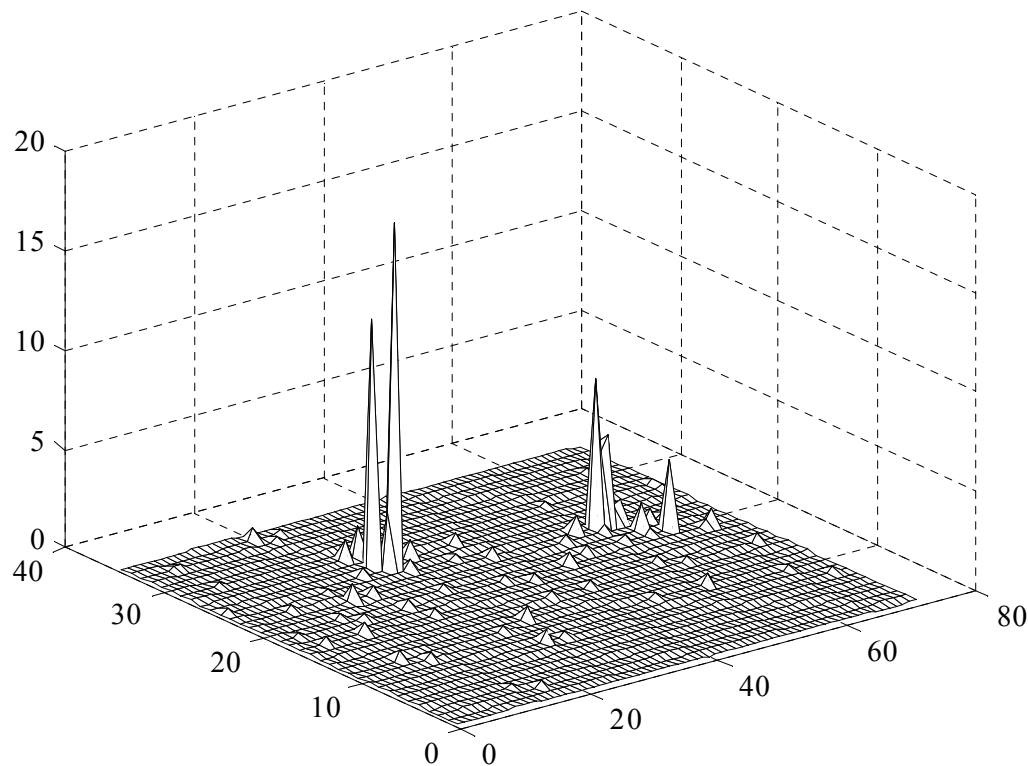
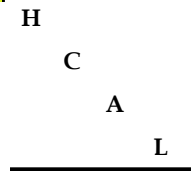
MLLA - Numerical



Numerical results were calculated. $\langle n \rangle$ increases rapidly with cone angle up to ~ 0.8 . We expect ~ 30 hadrons in the jet at $M=700$ GeV., ~ 12 at $M = 120$ GeV. We can use $D(z,M)$ as a guide to pileup in extracting jets. Basically angular ordering means that soft jet fragments occur at wide angles w.r.t. the parton axis.



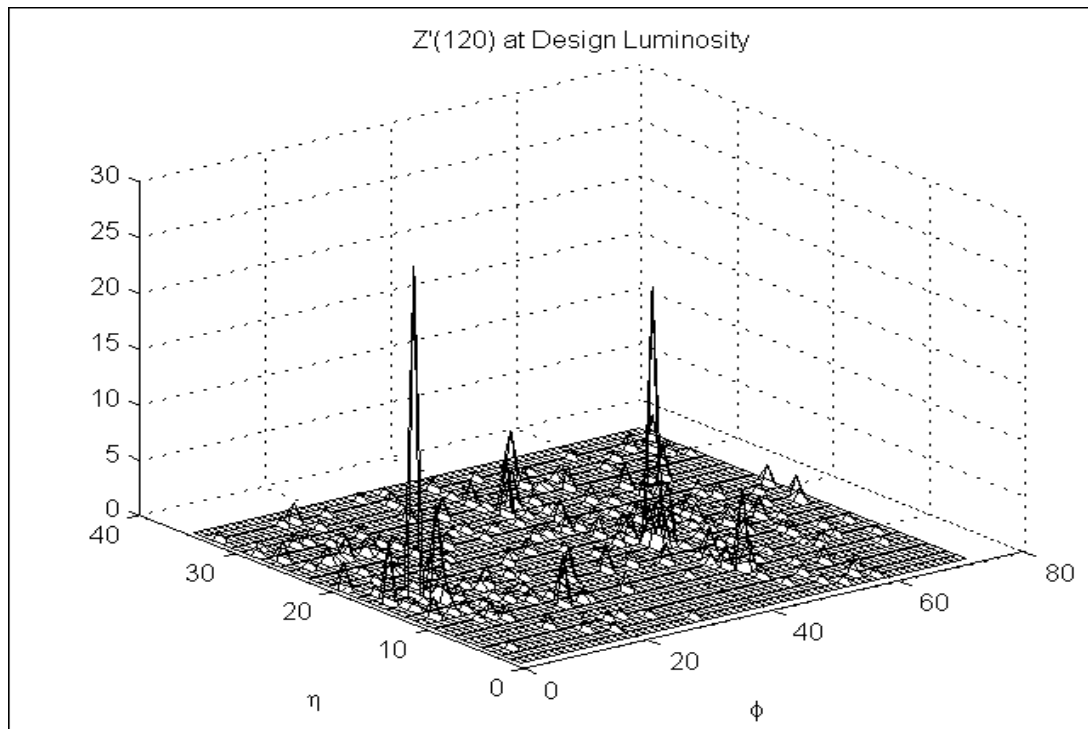
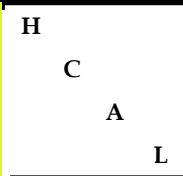
$Z'(120)$ Clustering at Low L



20 seeds > 1 GeV. 8 cones, $R = 0.9$, 8 jets, $R_{sep} = 0.9$. 27, 19 clusters ($E_t > 0.5$ GeV in 2 highest E_t jets). Find all seeds, then attach all clusters to cones, R_c , centered on seeds. Finally merge cones within R_{sep} . $E_{tj1} = 49$ GeV, $E_{tj2} = 37.9$ GeV, $M_{jj} = 85$ GeV



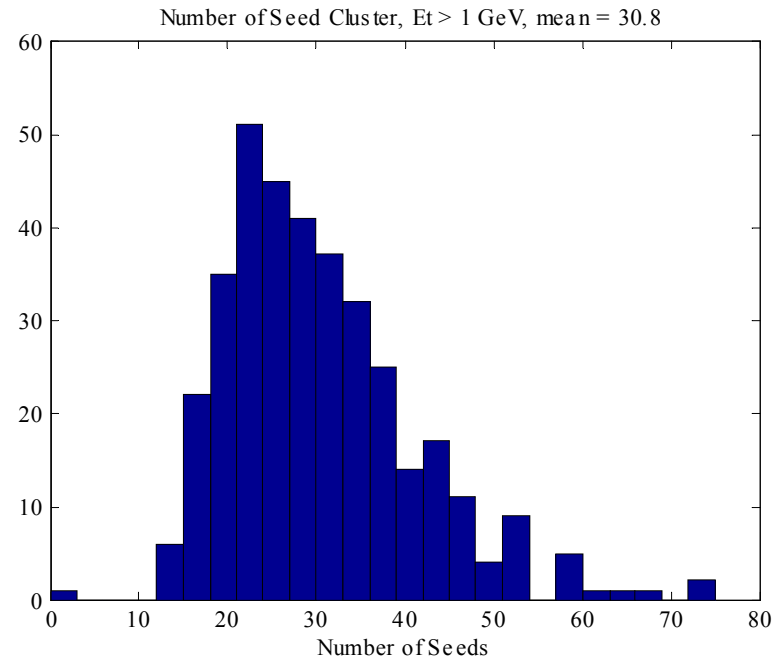
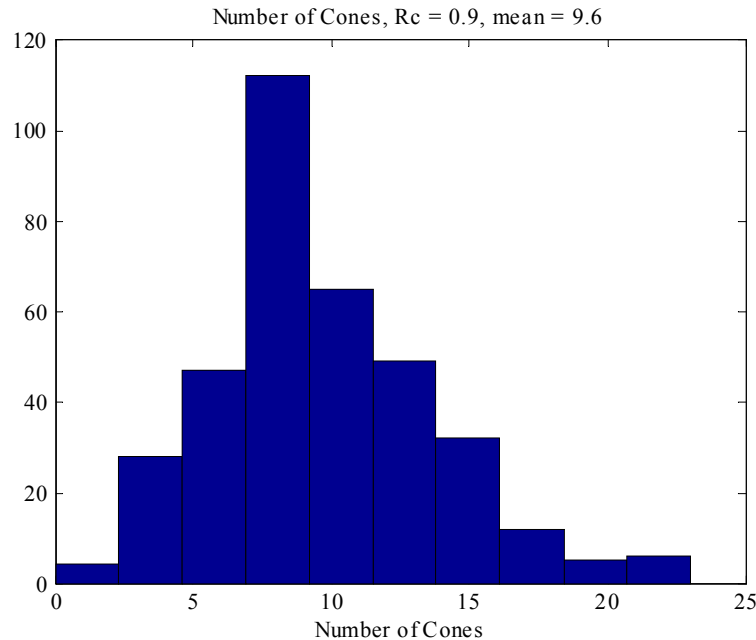
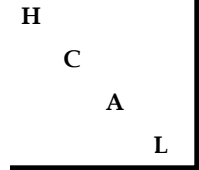
$Z'(120)$ at Design L



**Clearly, towers are still sparsely populated.
Equally clearly, we need to work harder to
preserve the dijet mass resolution.**



Seeds, Clusters, Cones



$\langle N_s \rangle = 30.8/\text{event}$

$\langle N_c \rangle = 9.6/\text{event}$

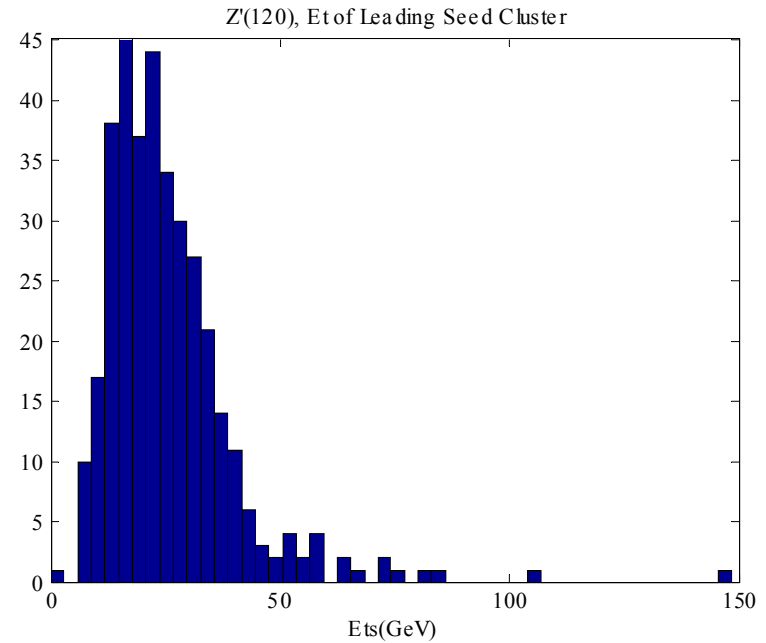
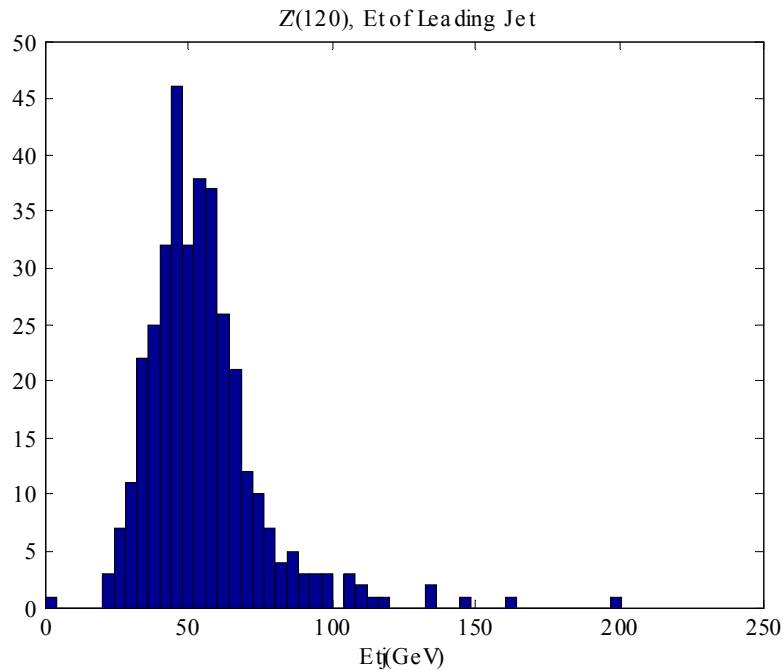
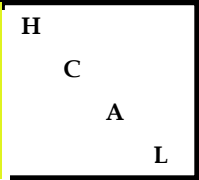
$\langle N_j \rangle = 9.3/\text{event}$

$E_{ts} > 1.0 \text{ GeV}$, $E_{tc} > 0.25 \text{ GeV}$, $R_c = 0.9$, $R_{sep} = 0.9$.

There are many jets if seed threshold is made low.



Leading Jet



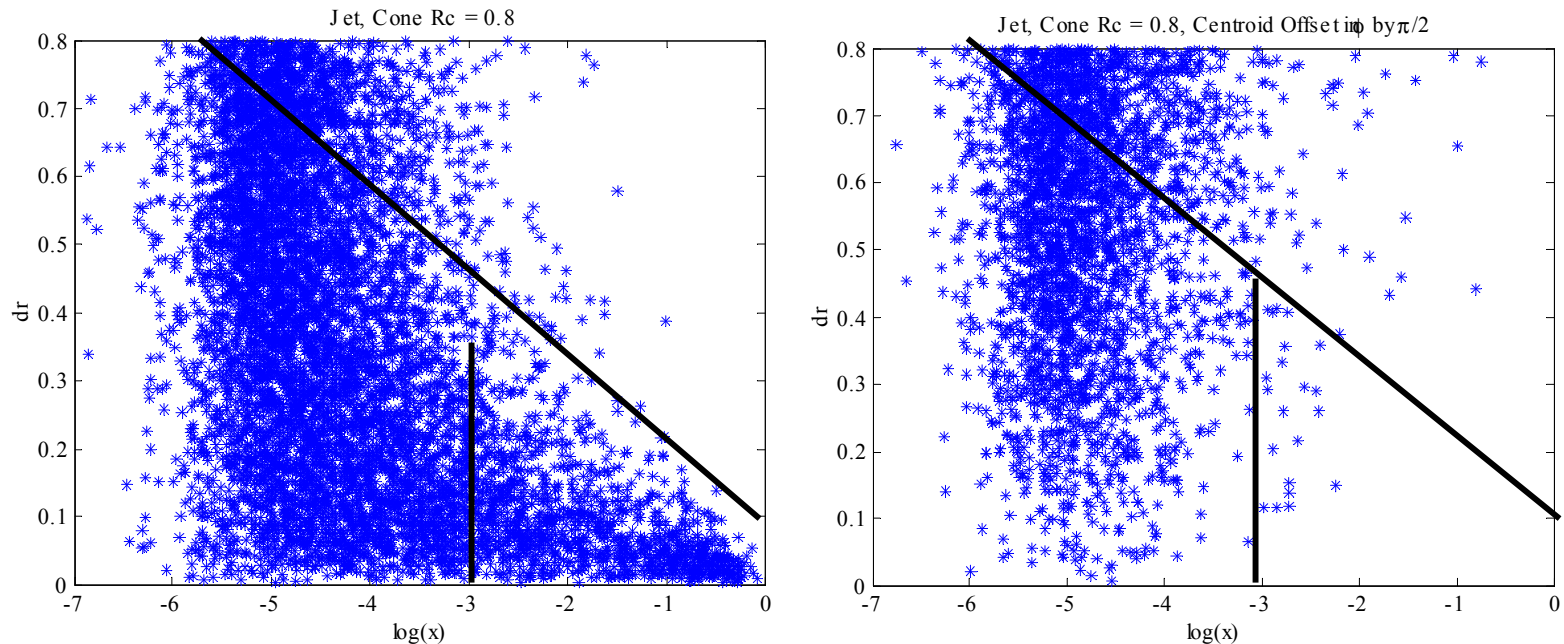
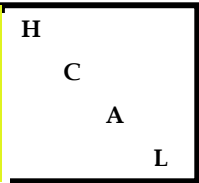
$\langle N_s \rangle_{j1} = 21 = \# \text{ clusters in lead jet}$

$\langle Et \rangle_{sj1} = 25.0 \text{ GeV} = \text{Et of seed cluster in lead jet}$

$\langle Et \rangle_{j1} = 55 \text{ GeV} \text{ (45.0 GeV for j2)}$



Pileup in $Z'(120)$ at Low L

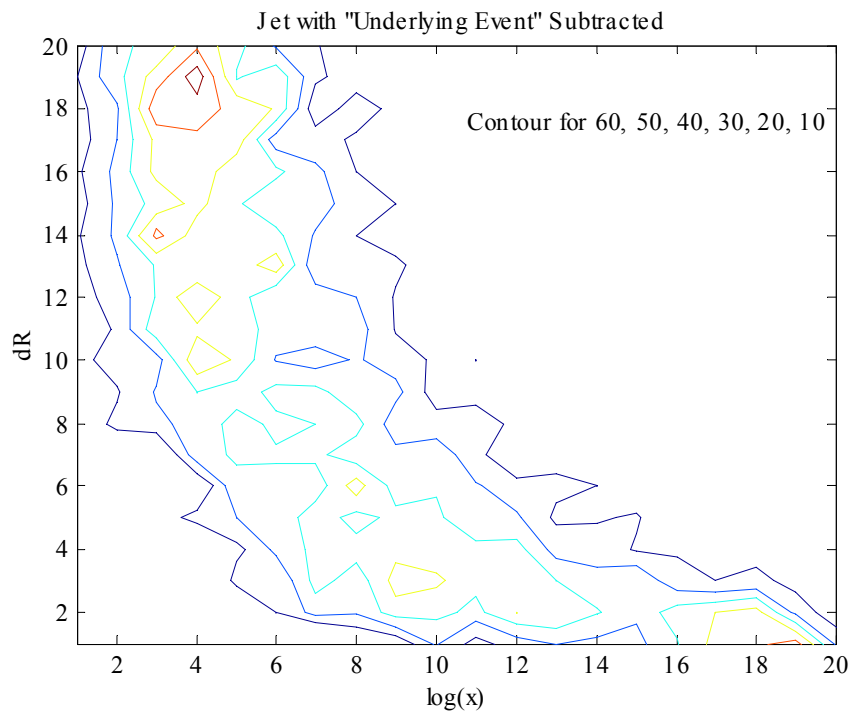
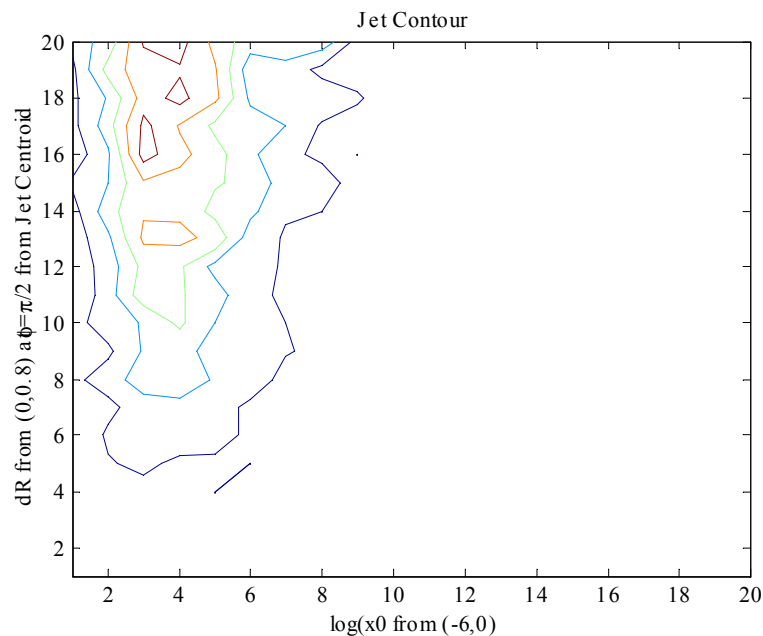
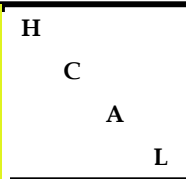


Use $\log(x)$ as the appropriate variable (MLLA). The jet shows the small angle, high momentum component. A cone at 90 degrees to the jet shows soft and wide angle underlying event and pileup behavior. Cuts are picked for high L.

The sigma/mean is 17.8% at low L.



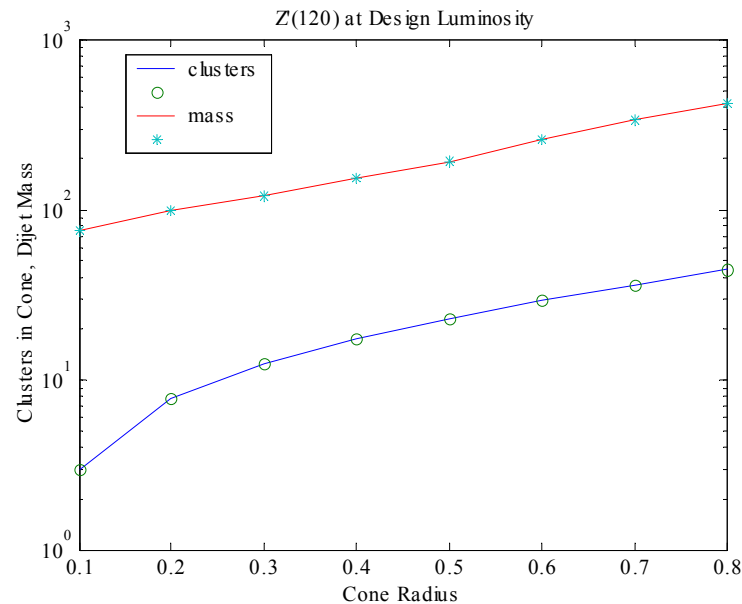
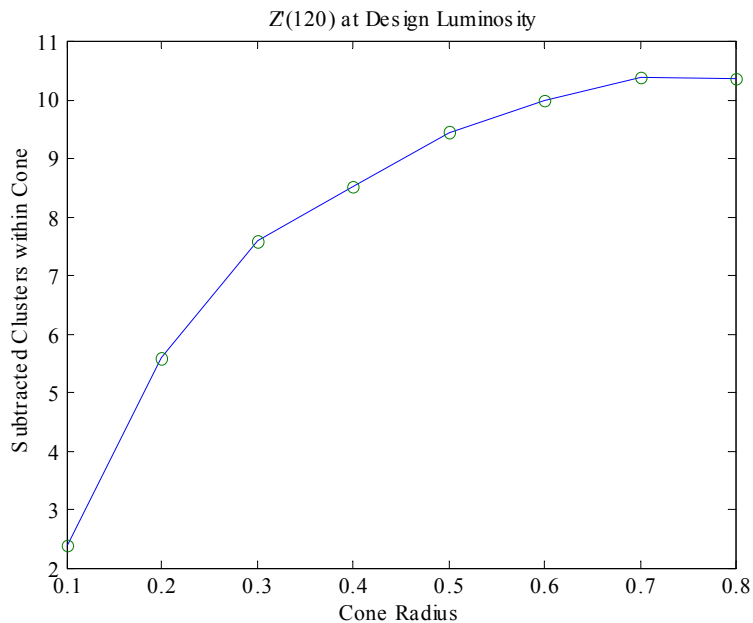
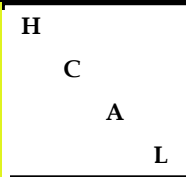
Contours in $Z'(120)$



Estimate the true contour in $(\log x, dR)$ for a jet by subtracting the cones contour at 90 degrees to the jet for $Z'(120)$ at low L. The pileup and the jet populate different regions of the energy-angle flow phase space.



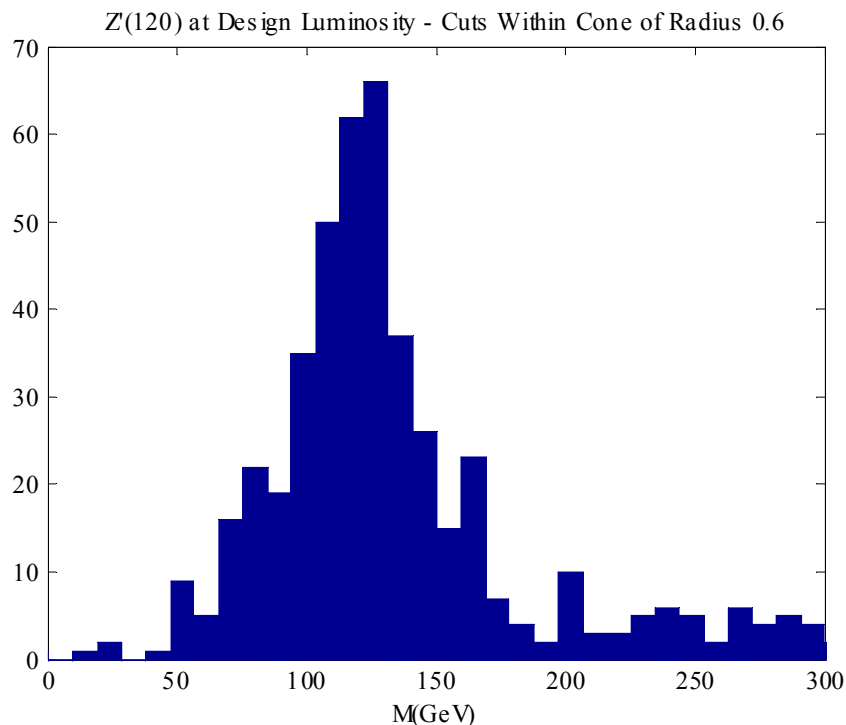
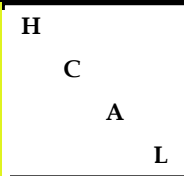
Pileup Subtraction



Must go to cone radius ~ 0.6 to capture all the jet fragments on average. However, the number of clusters is ~ 29 then (10.3 real + 18.3 pileup) and the mean dijet mass is 258 GeV



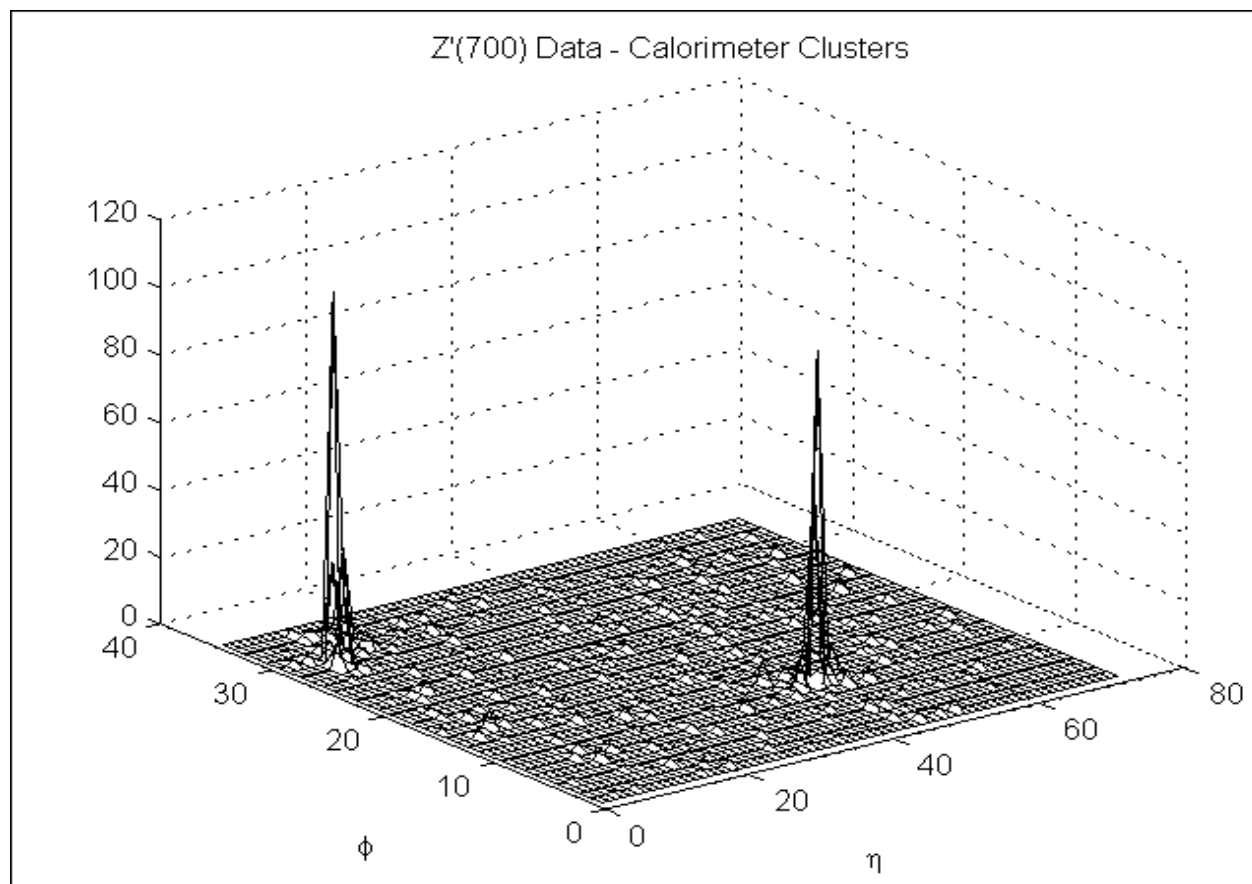
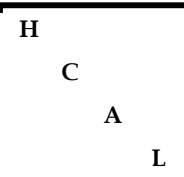
$Z'(120)$ at Design L



After cuts on dR and $\log x$ the fitted mean is 119 GeV with a fitted sigma = 20.26 GeV or sigma/mean = 17.0 %. Thus the dijet mass resolution is maintained at design L. There is some residual high mass tail, however.

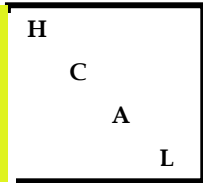


$Z'(700)$ at Design L





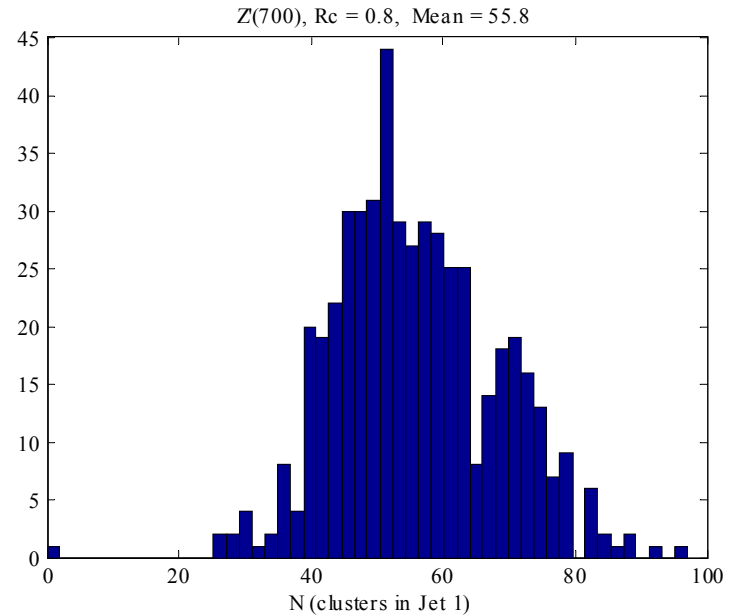
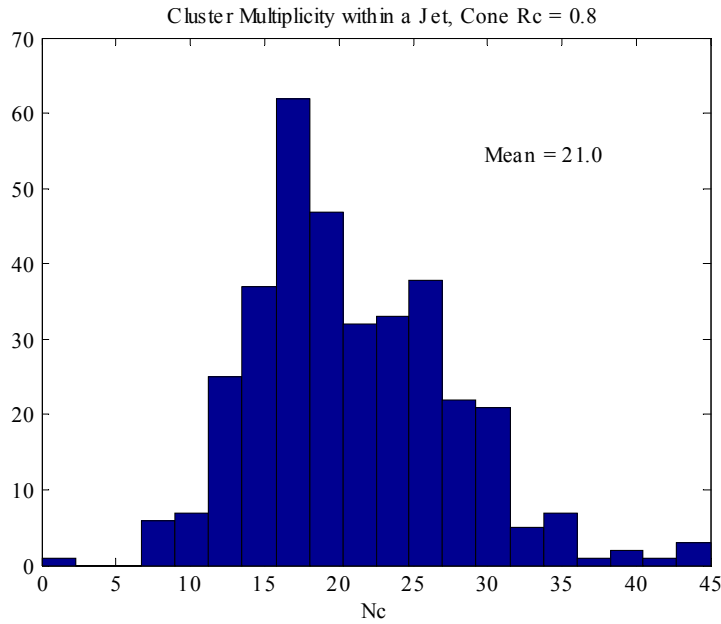
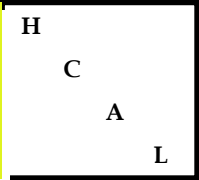
$Z'(700)$ at Design L



- **Seed $E_t > 10$ GeV, $\langle N_s \rangle = 10.4$, $\langle ET_{s1} \rangle = 198$ GeV (leading seed cluster).**
- **Cone $R_c = 0.8$, $\langle N_c \rangle = 3.33$**
- **Jet – Merge Cones, $\langle N_j \rangle = 2.72$**
- **Clusters in Jet - $\langle N_{cl} \rangle = 55.5$**
- **Clusters at 90 degrees to jet, $\langle N_{clo} \rangle = 36.4$. Difference = 19.1 (expect more in LLA, but there may be cluster merging at high density within the jet).**
- **$\langle Et_{j1} \rangle = 352.2$ GeV**



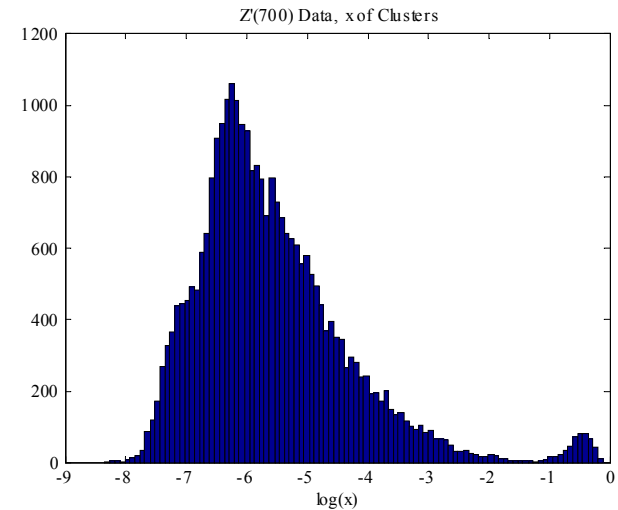
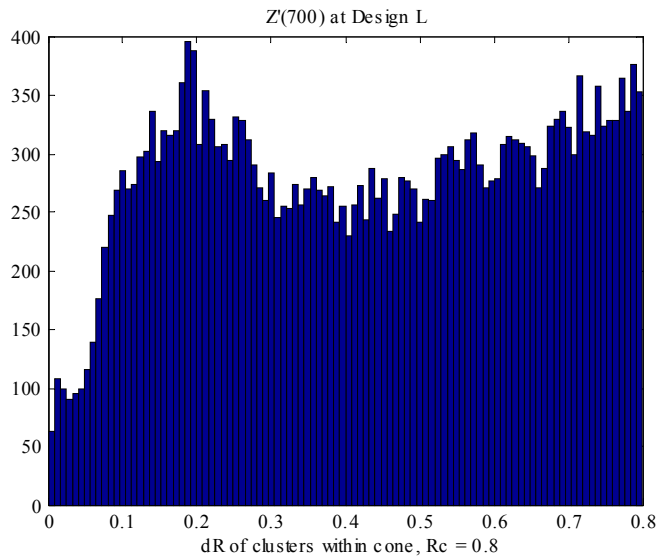
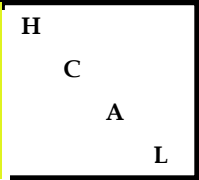
Clustering



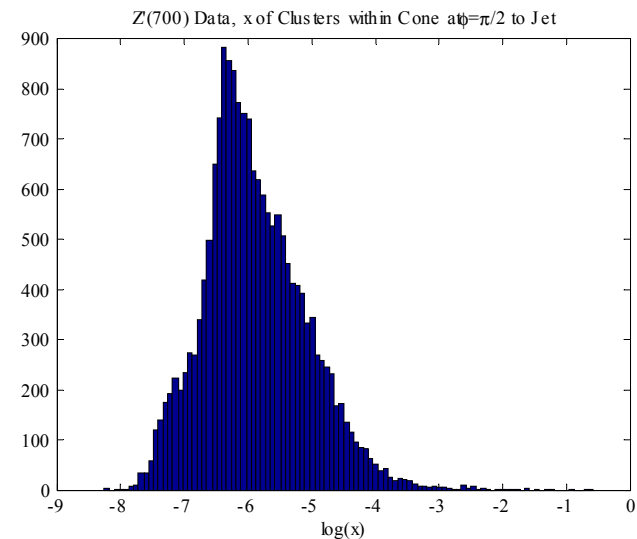
For $Z'(120)$ there are 24 clusters, $R_c = 0.9$, within the jet and 10 at 90 degrees – leading to 14 after subtraction. This is close to MLLA estimates. For $Z'(700)$ at design L, the number of clusters within a cone is much larger due to pileup, 55.8. For 1/5 luminosity it is 21 clusters. For design luminosity it is $\sim 56 - 36$ clusters or ~ 19 .



dR and log(x) for Z'(700)

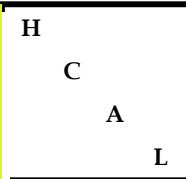


Clearly the pileup has $dN dR \sim R$ (area), while the jet shows a peak at $R \sim 0.2$. The pileup is at low x , while there is a peak at high x .

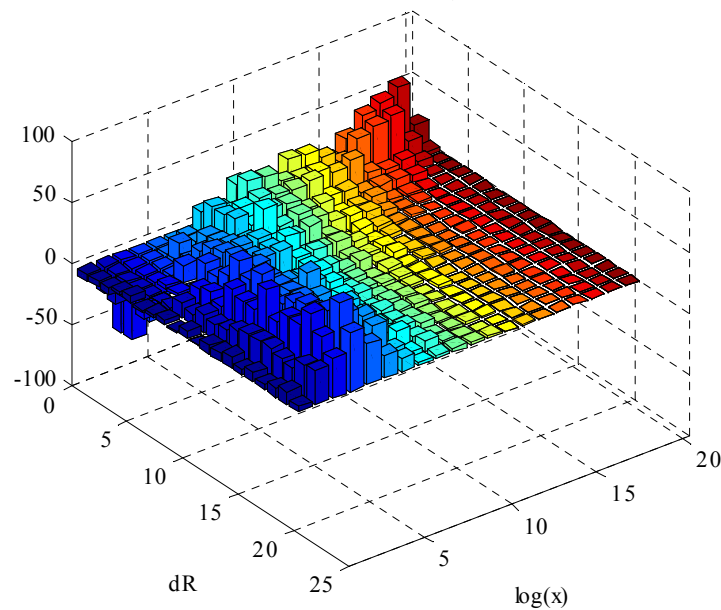




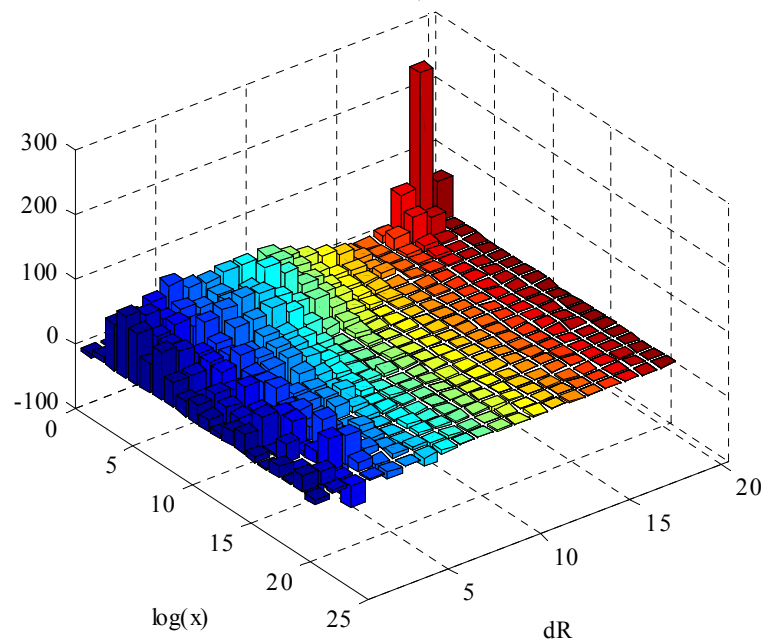
Pileup Subtracted ($\log x, dR$) Jet contours



Jet With "Underlying Event" Defined at $\phi = \pi/2$ to Jet Subtracted



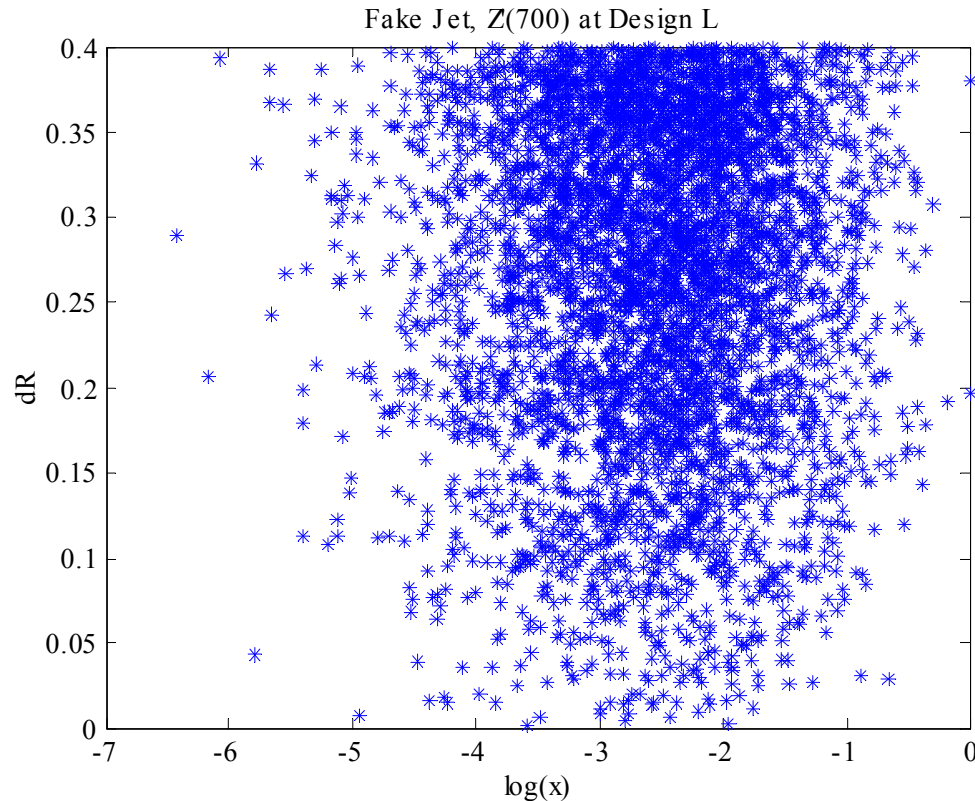
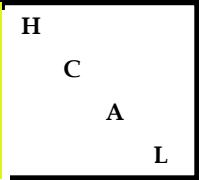
Z'(700) Data, ($dR, \log(x)$), $\phi = \pi/2$ "Jet" Subtracted



For both $Z'(120)$ at low L and for $Z'(700)$ at design L there is a core of the jet at small dR and large x .



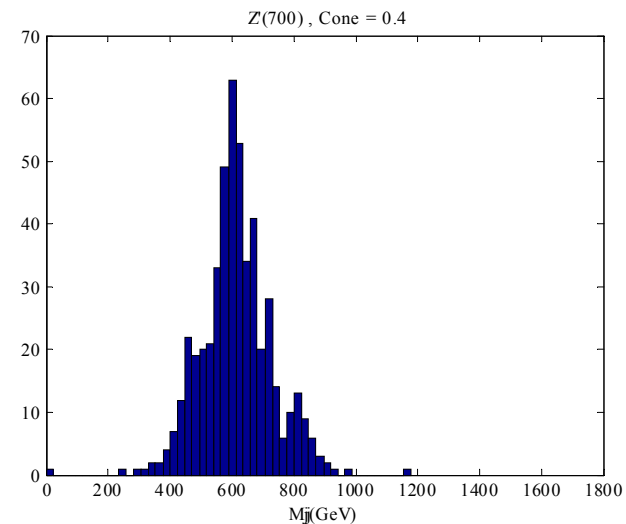
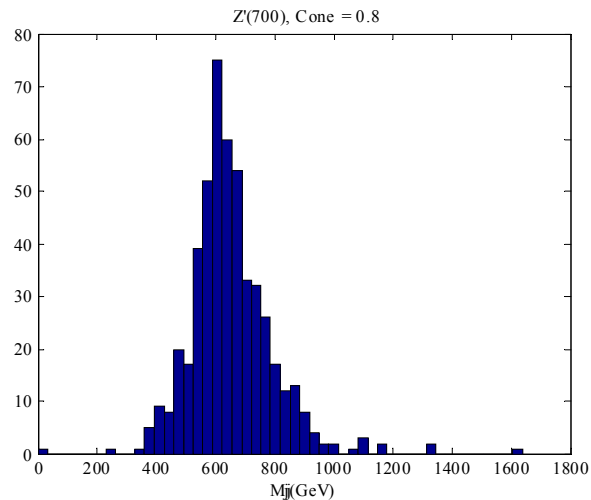
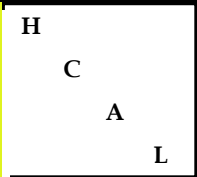
Fake Jets at Design L



Look at fake jets by taking cone at 90 degrees to jet at design L and normalizing x now to total E_t within that cone. There is no jet “core” of high momentum at small angles.

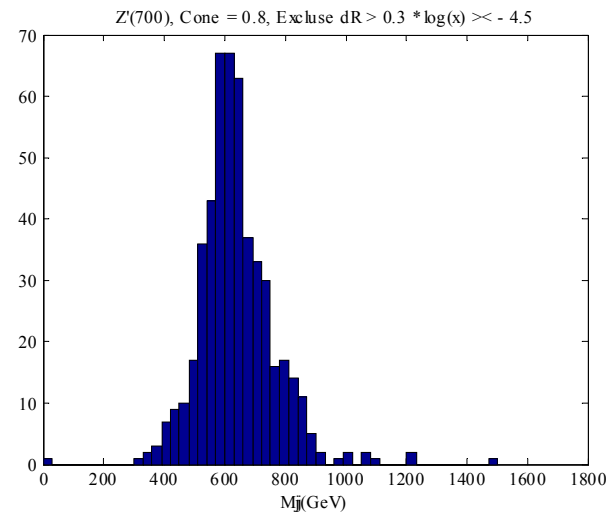


Dijet Mass in $Z'(700)$



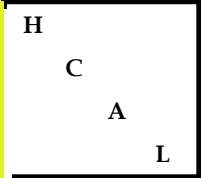
**Mean ~ 614 GeV,
sigma ~ 74 GeV. No
major improvements.**

**$R_c = 0.4$ or $\log(x) > -4$
or a combined cut all
about the same.**





Conclusions



- The pileup at design luminosity is not too severe for $Z'(700)$.
- The appearance of a low P_t inclusive pileup \sim uniform in cone area is confirmed.
- Pileup for $Z'(120)$ is severe but it can be alleviated with well designed cuts on energy – angle flow within the jet. More incisive cuts than just a small cone or a threshold work well.
- Direct subtraction event by event does not work well.